

# Modeling Structured Event Streams in System Level Performance Analysis

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# Outline

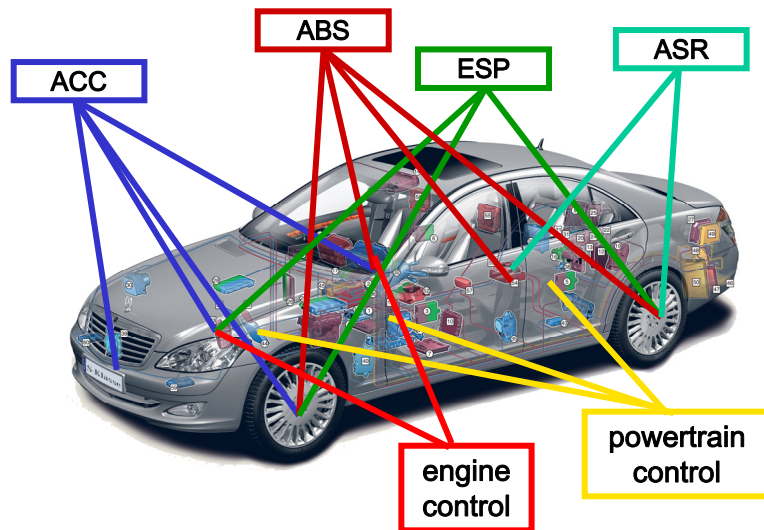
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- **Motivation**
- **Modular Performance Analysis with Real-Time Calculus**
- **Approach 1: FIFO Scheduling**
- **Approach 2: Event Count Curves**
- **Comparison / Case Study**
- **Conclusion**

# Motivation

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## Distributed Stream-based Embedded Systems



Design and analysis are complex due to:

- Concurrency
- Interference on shared resources
- Non-determinism in timing

Requirements for Performance Analysis:

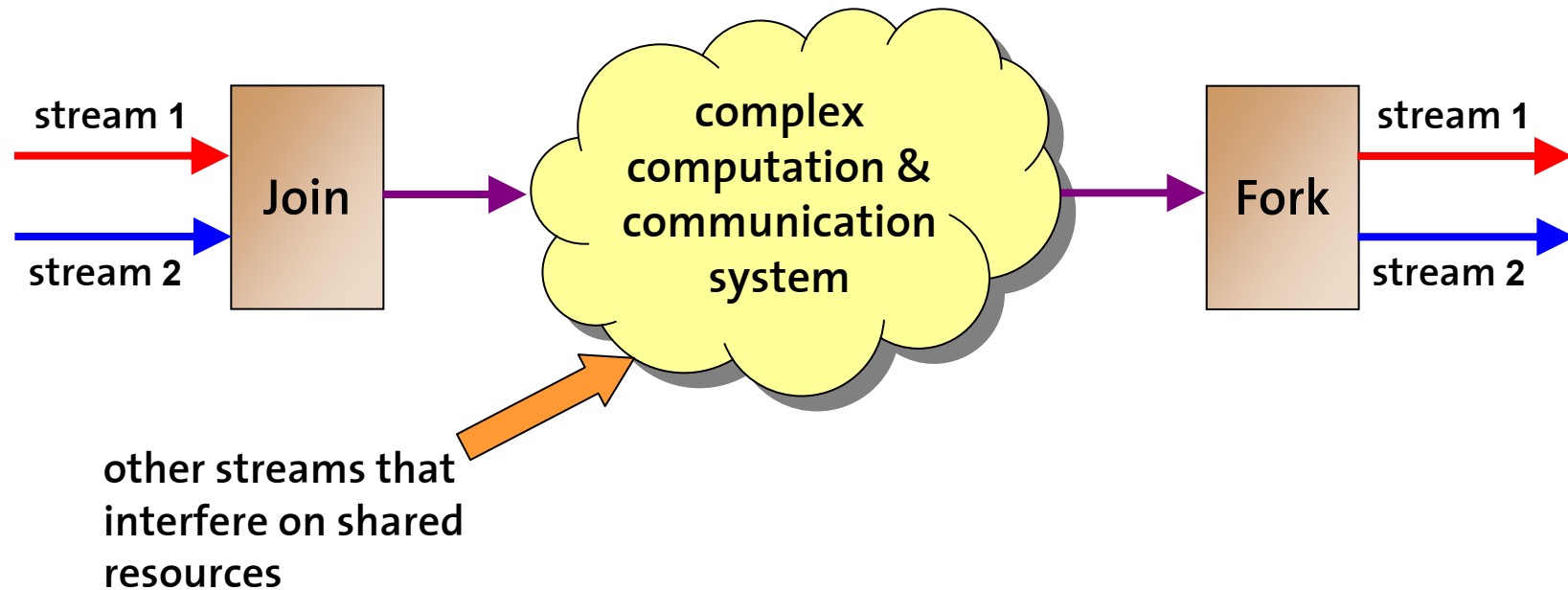
- Coverage of system behaviors
- Accuracy of results
- Computational efficiency

Analytic methods for Modular Performance Analysis: • MPA-RTC (ETHZ)  
• SymTA/S (TUBS)

# Motivation

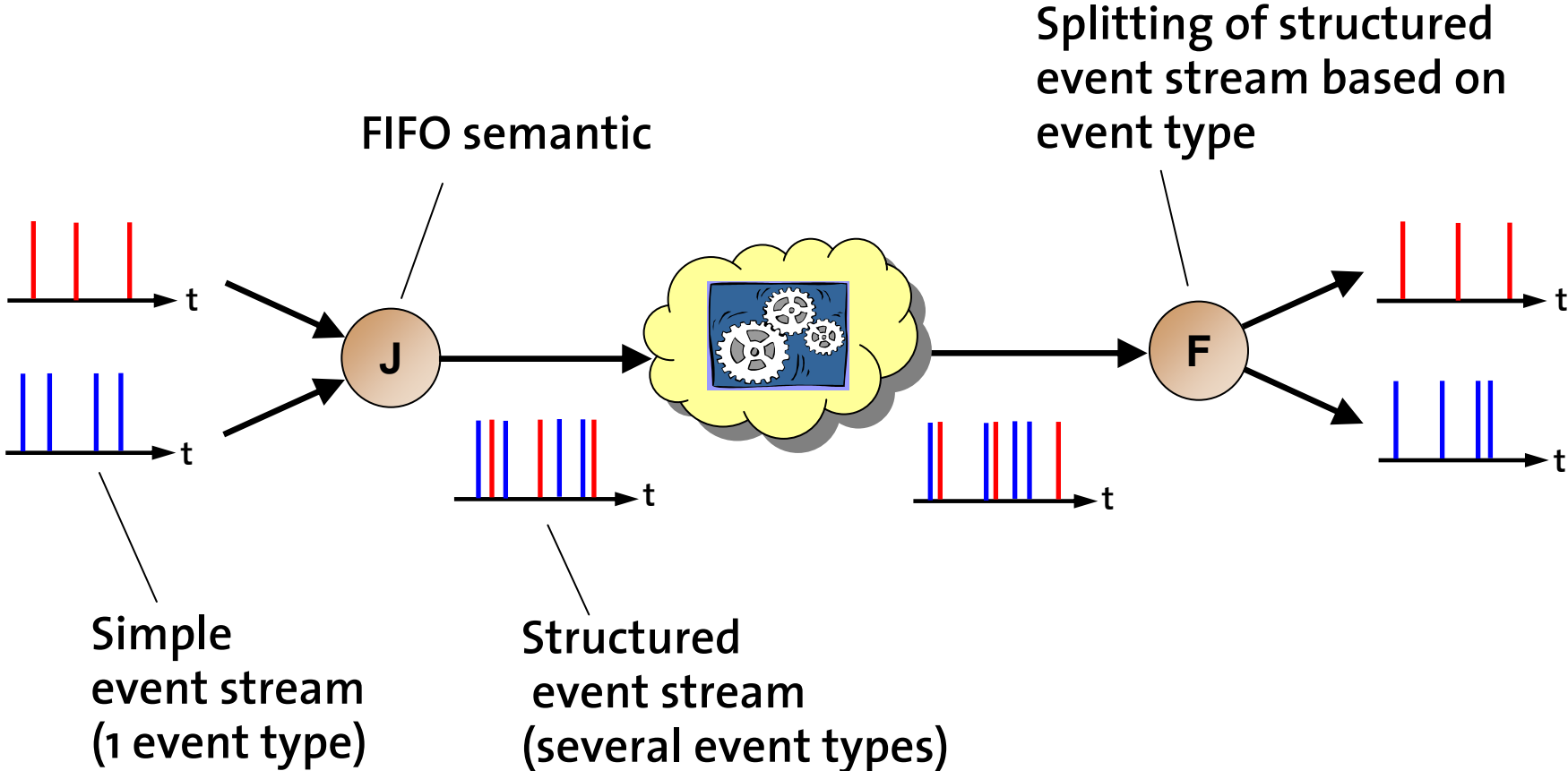
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Relevant design pattern: Join and Fork of event or data streams



Goal: Extend analytic methods for performance analysis such that join/fork operations on streams can be captured accurately

# Definitions

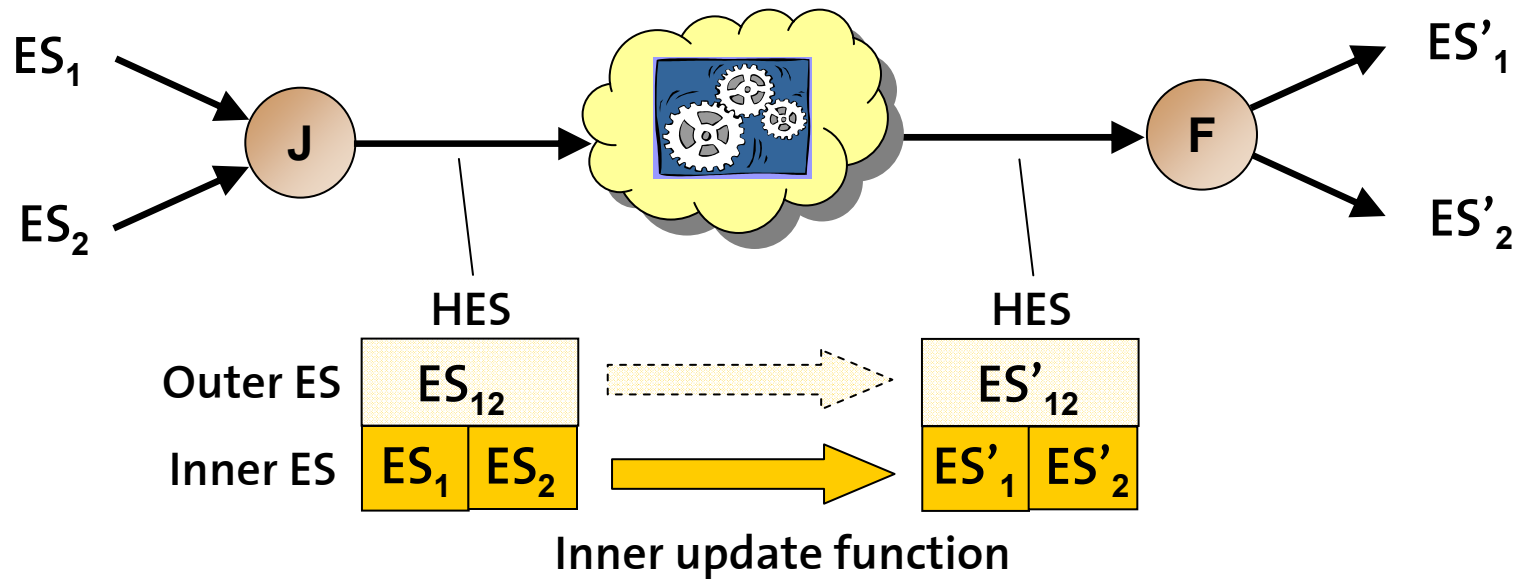


Event type = provenance

# Related Work

## Hierarchical Event Model (TU Braunschweig)

J. Rox & R. Ernst, *Modeling Event Stream Hierarchies with Hierarchical Event Models*, DATE 2008



- Limitations:
- Method is not transparent to existing component models
  - Deep processing of HES required by component models

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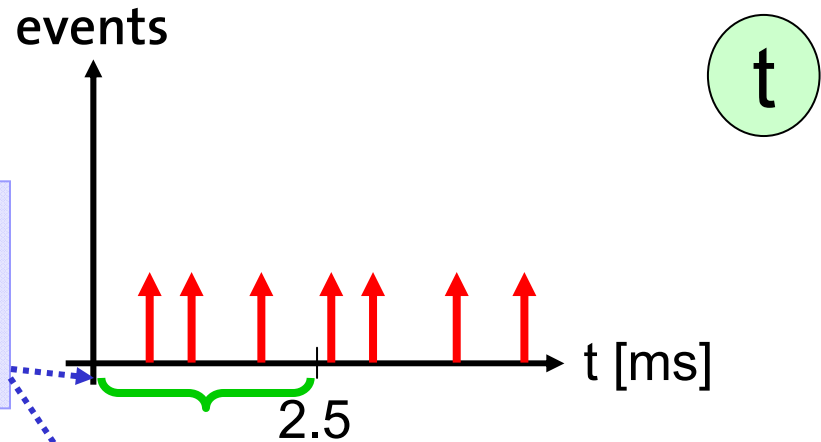
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# Arrival Curves

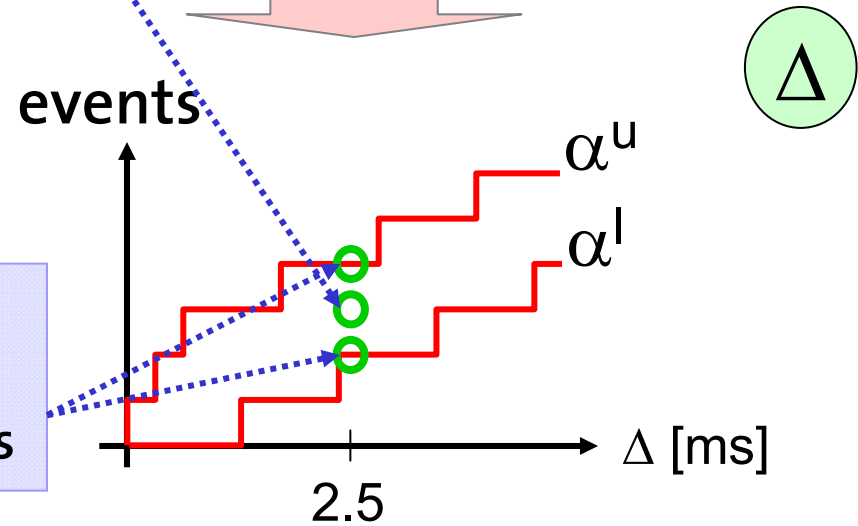
Event Stream

number of events in  
in  $t=[0 .. 2.5]$  ms



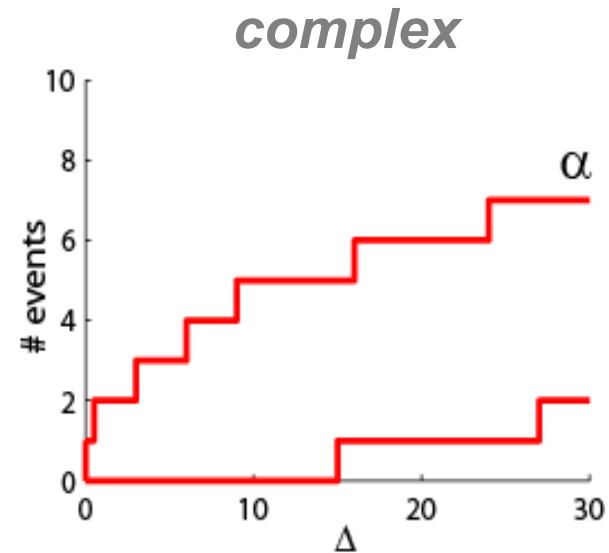
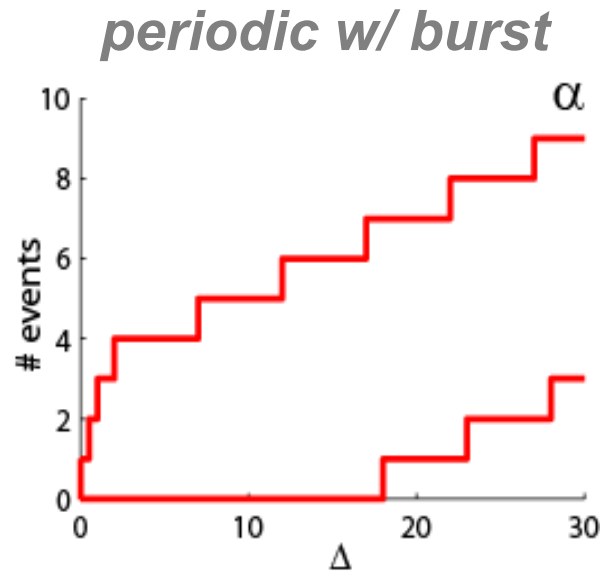
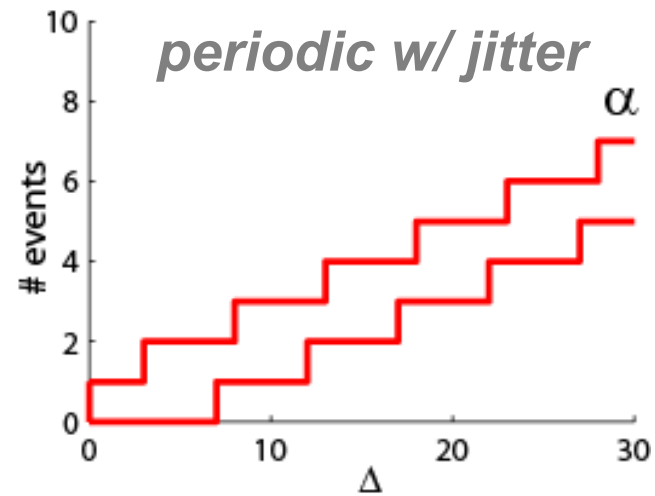
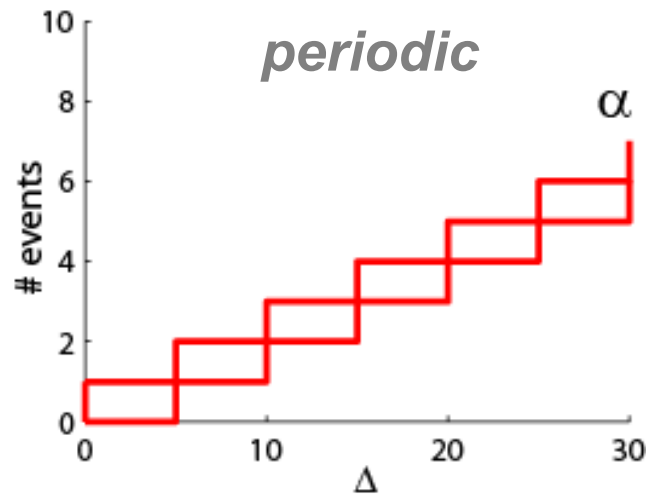
Arrival Curves  $[\alpha^l, \alpha^u]$

maximum/minimum  
arriving events in *any*  
*interval* of length 2.5 ms



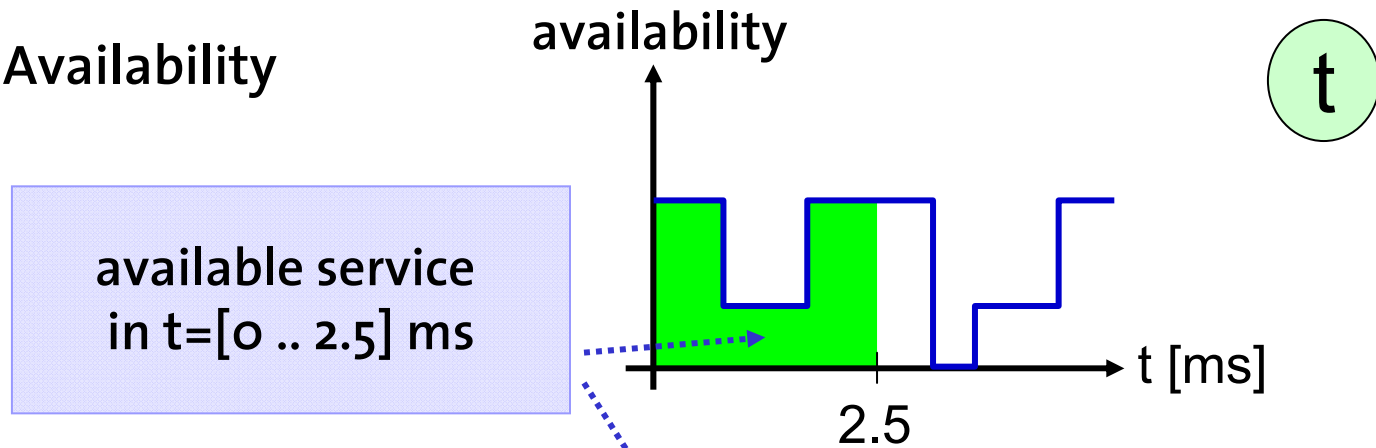


# Examples of Arrival Curves

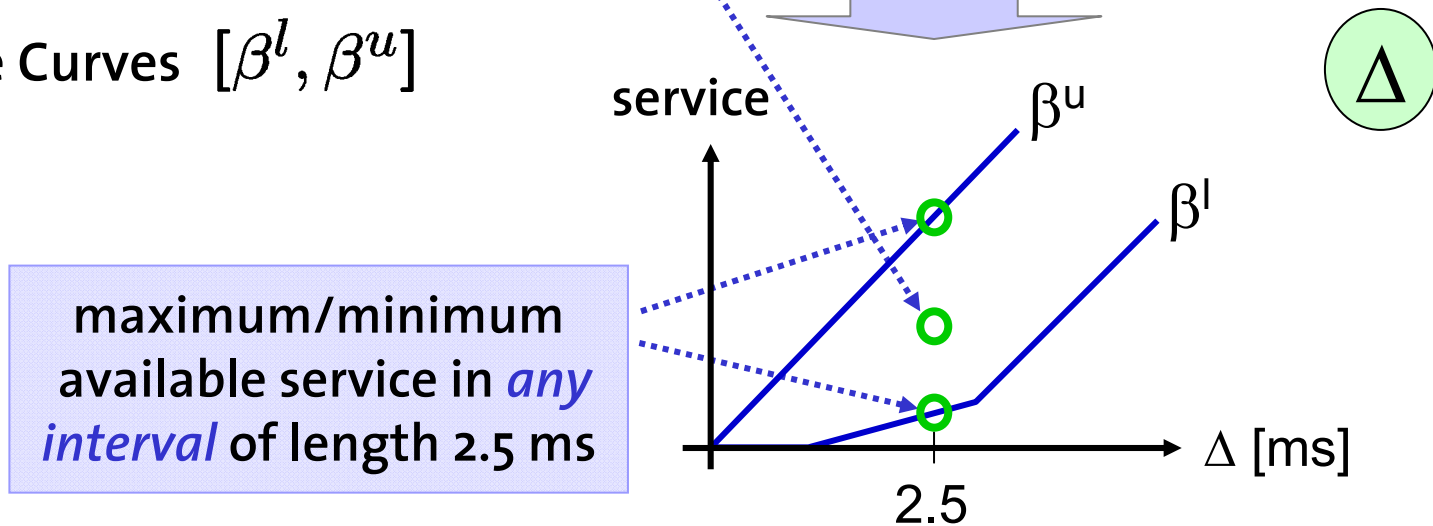


# Service Curves

Resource Availability

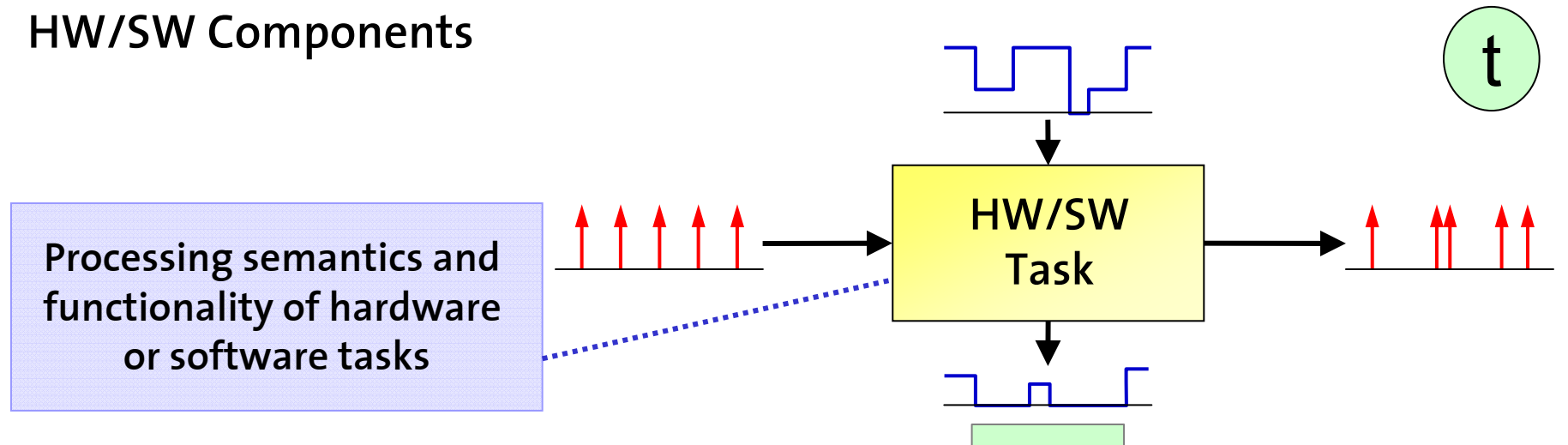


Service Curves  $[\beta^l, \beta^u]$

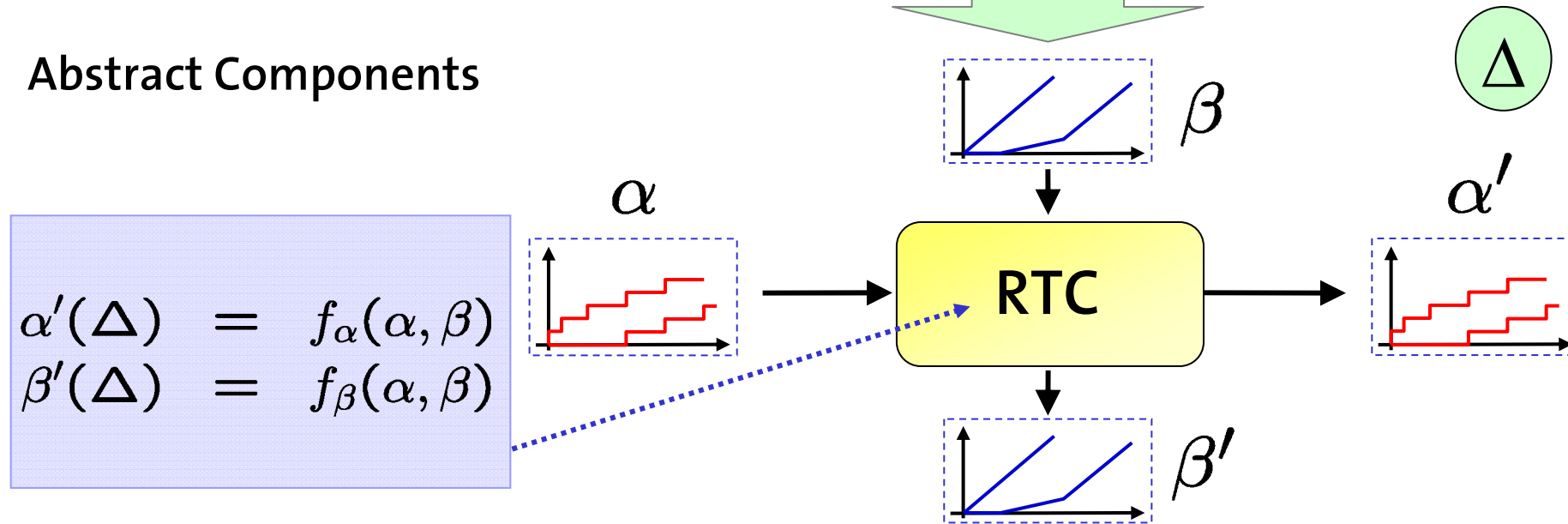


# Processing Model (HW/SW)

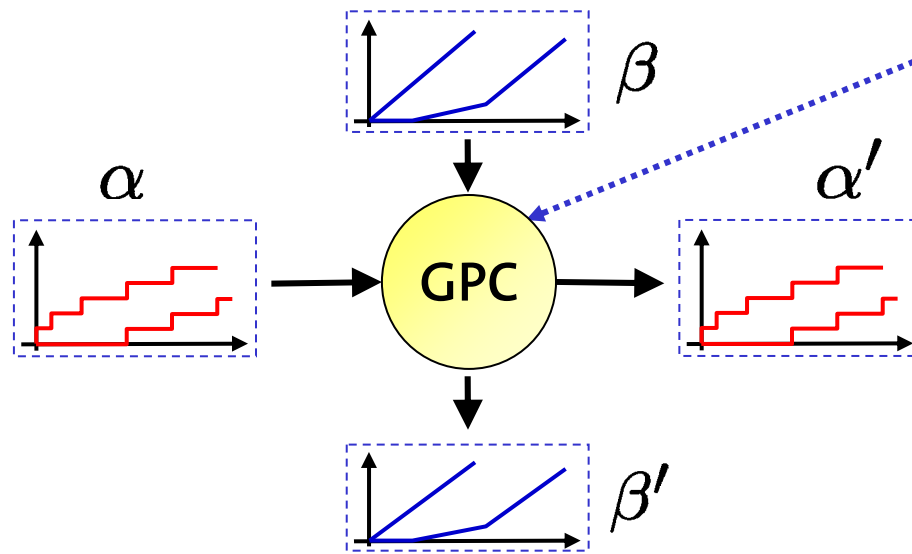
## HW/SW Components



## Abstract Components



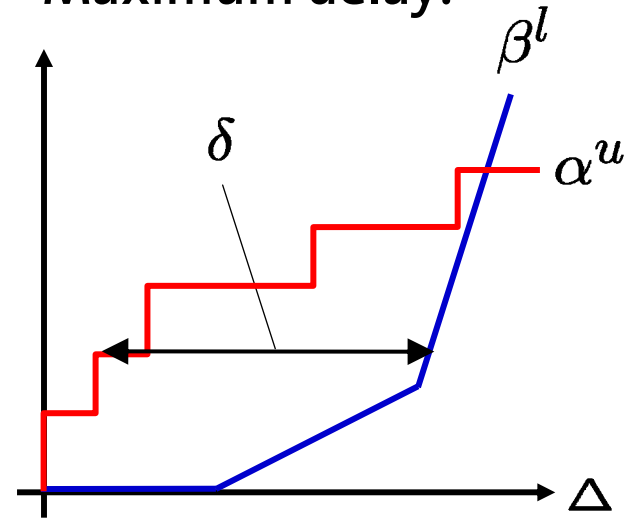
# Example: Greedy Processing Component (GPC)



$$\begin{aligned} \alpha'^u &= GPC_{\alpha'^u}(\alpha^u, \beta^u, \beta^l) \\ \alpha'^l &= GPC_{\alpha'^l}(\alpha^l, \beta^u, \beta^l) \\ \beta'^u &= GPC_{\beta'^u}(\beta^u, \alpha^l) \\ \beta'^l &= GPC_{\beta'^l}(\beta^l, \alpha^u) \end{aligned}$$

- FIFO input buffer
- Greedy event processing

Maximum delay:



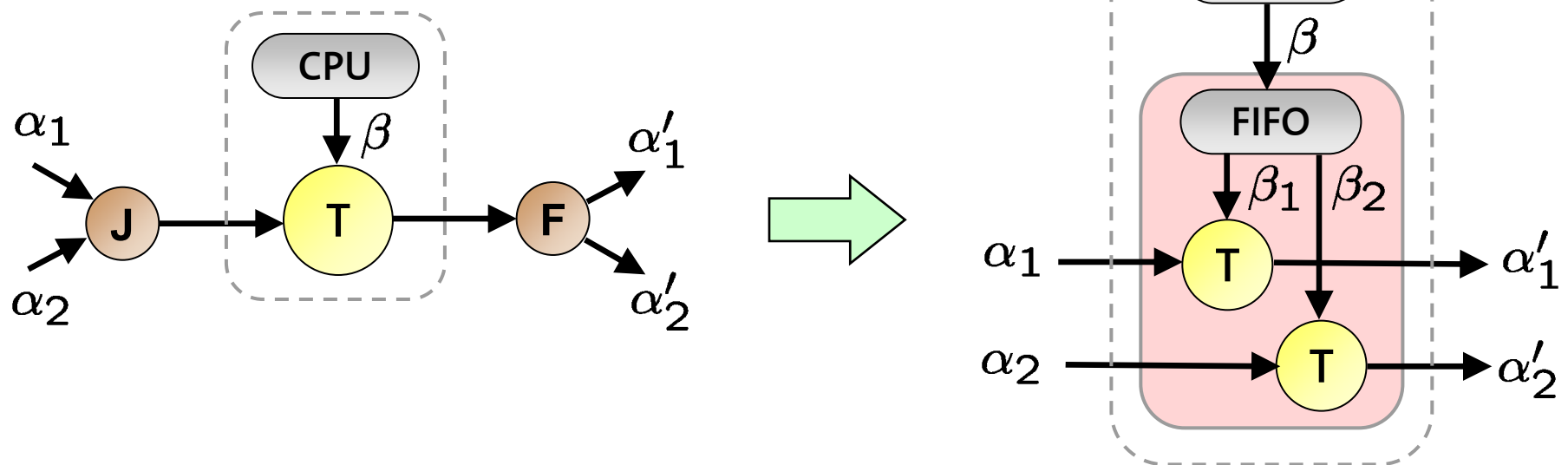
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- Modular Performance Analysis with Real-Time Calculus
- Approach 1: FIFO Scheduling
- Approach 2: Event Count Curves
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- Conclusion

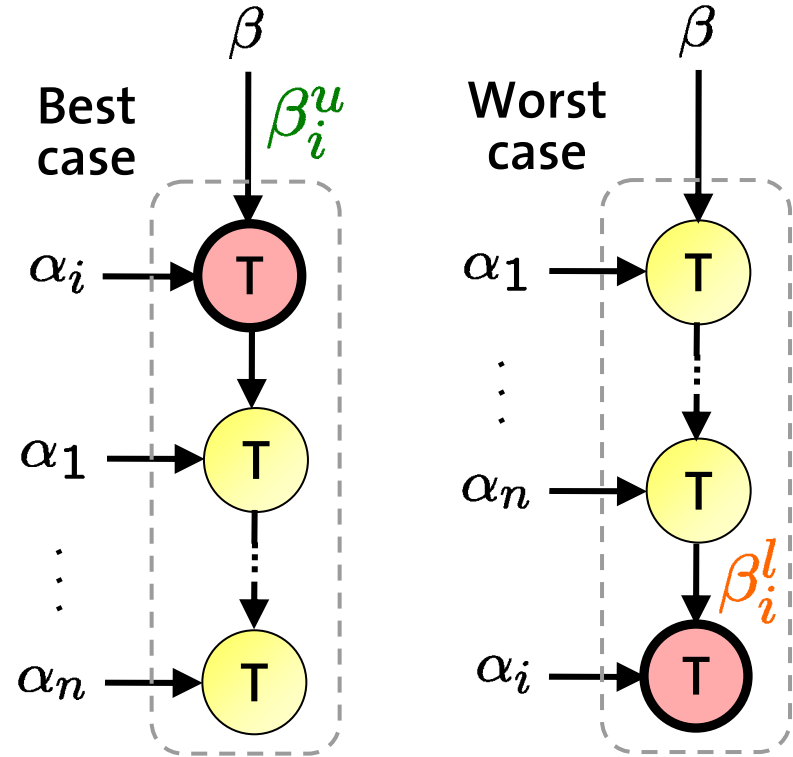
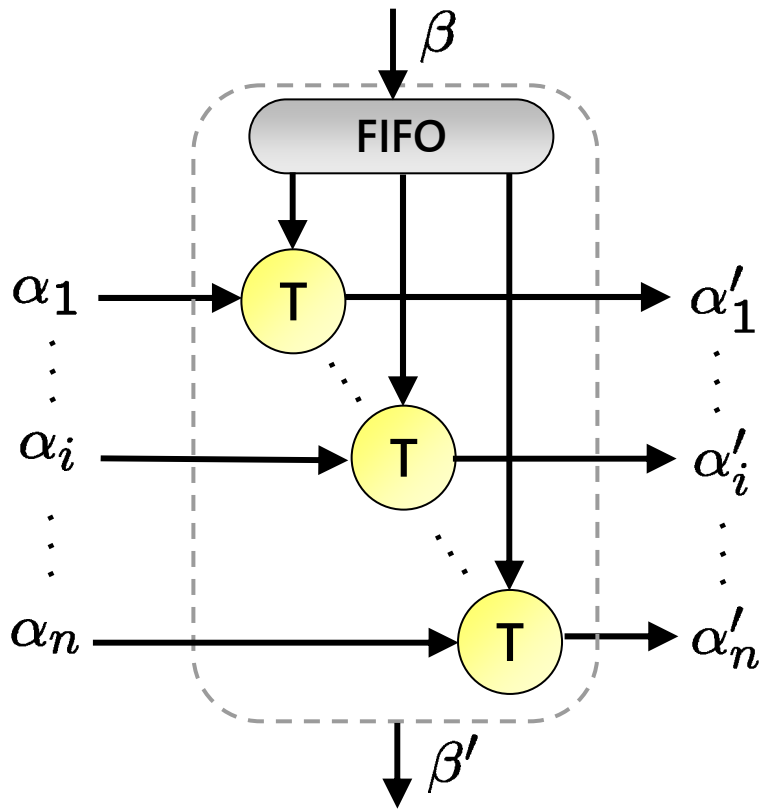
# FIFO Scheduling

- Keep sub-streams separated in the model
- Adapt existing component models



Modeling approach justified by FIFO semantics of Join operator

# FIFO Component in MPA



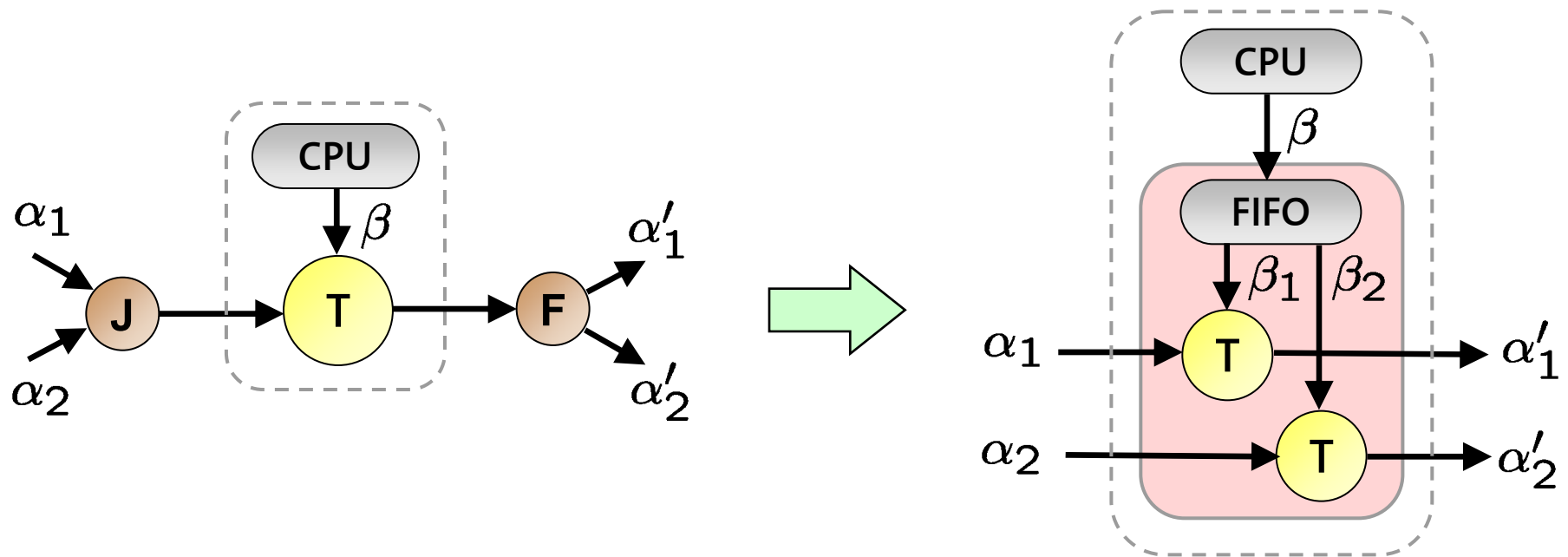
$$\beta^{lu} = GPC_{\beta^{lu}}(\beta^u, \sum_i \alpha_i^l)$$

$$\beta^{ll} = GPC_{\beta^{ll}}(\beta^l, \sum_i \alpha_i^u)$$

$$\alpha_i^{lu} = GPC_{\alpha_i^{lu}}(\alpha_i^u, \beta_i^u, \beta_i^l)$$

$$\alpha_i^{ll} = GPC_{\alpha_i^{ll}}(\alpha_i^l, \beta_i^u, \beta_i^l)$$

# FIFO Scheduling



Abstract processing component handles structure of input stream explicitly

⇒ Method is not transparent to existing component models!



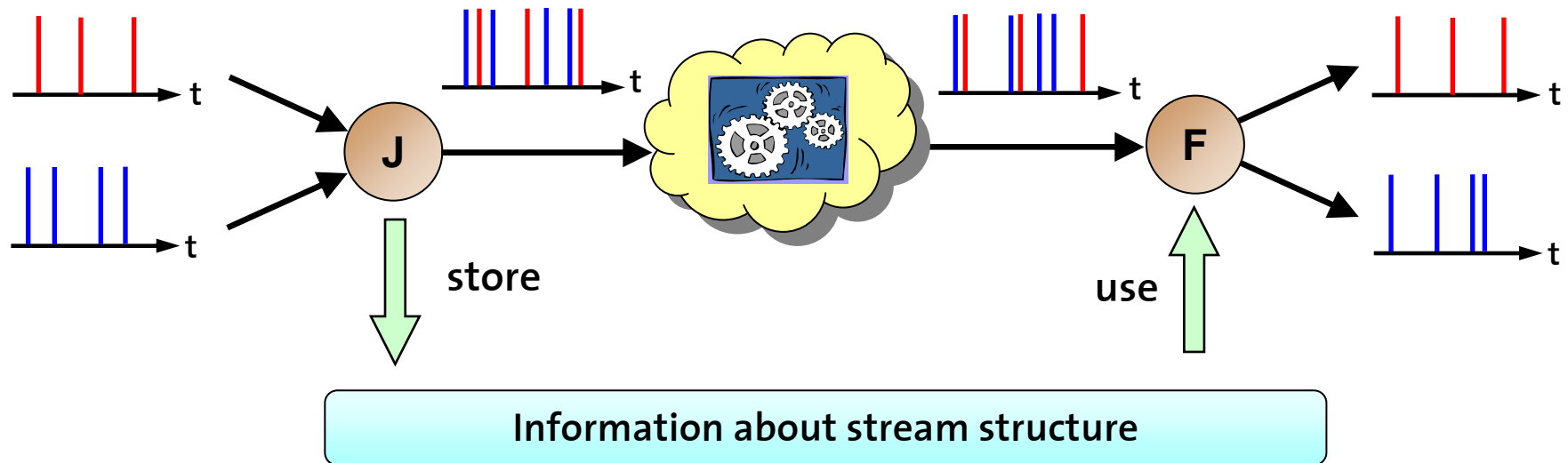
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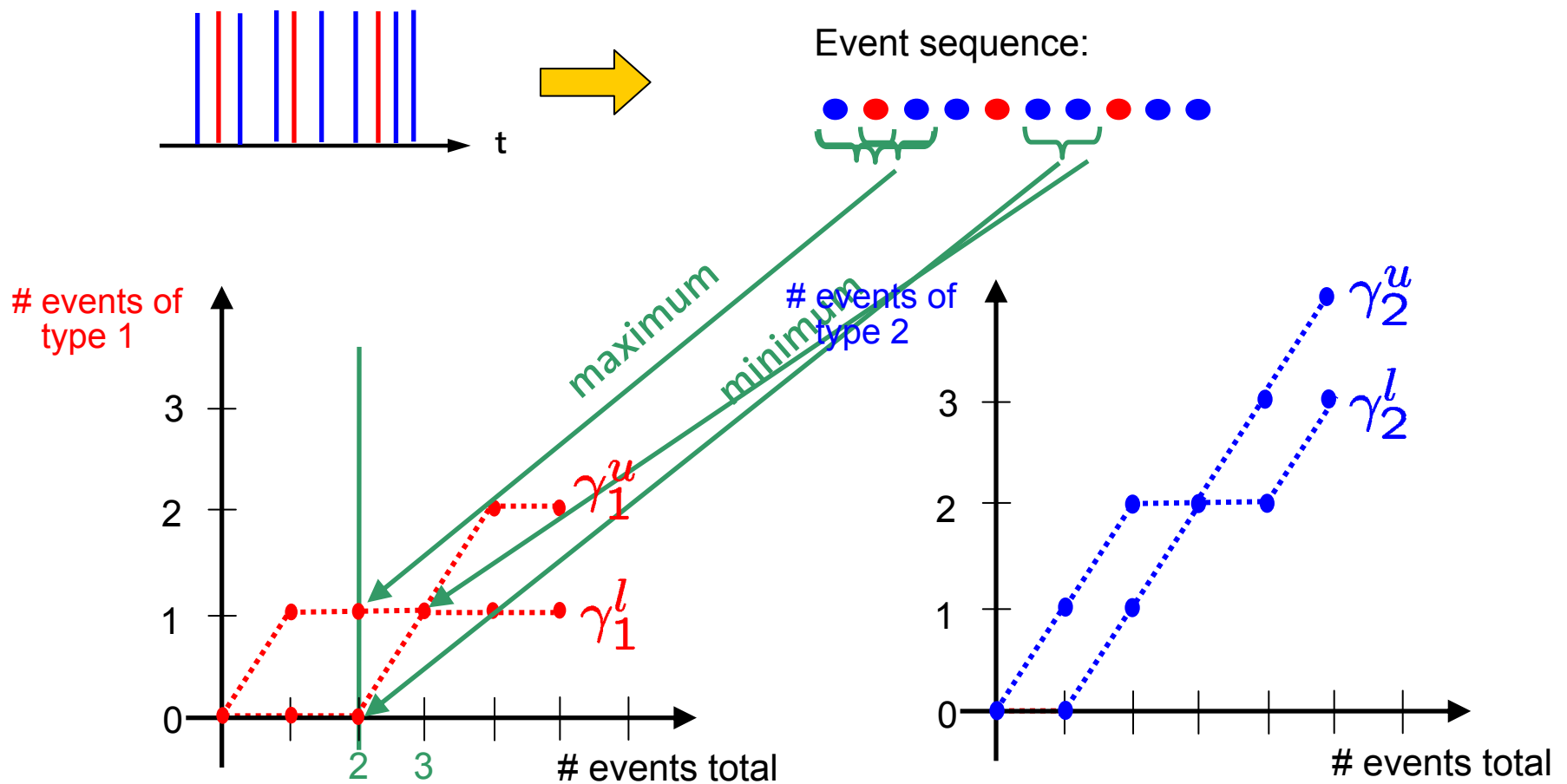
# Event Count Curves: Basic Idea

The processing components in MPA preserve the order of the events in a stream

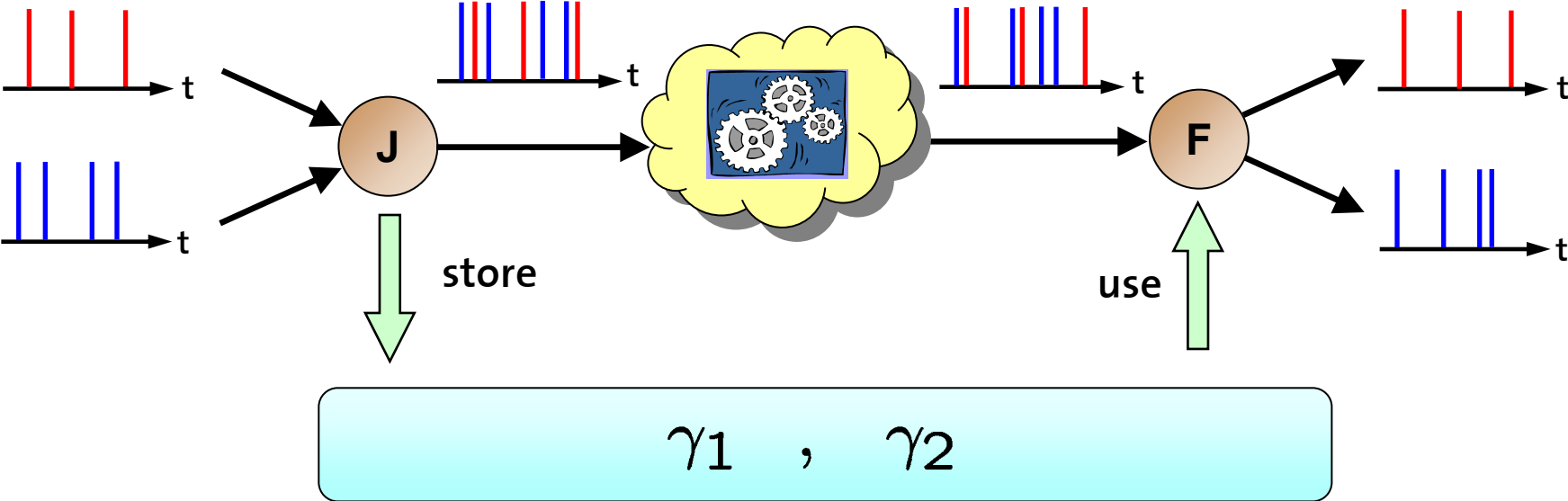


# Event Count Curves: Definition

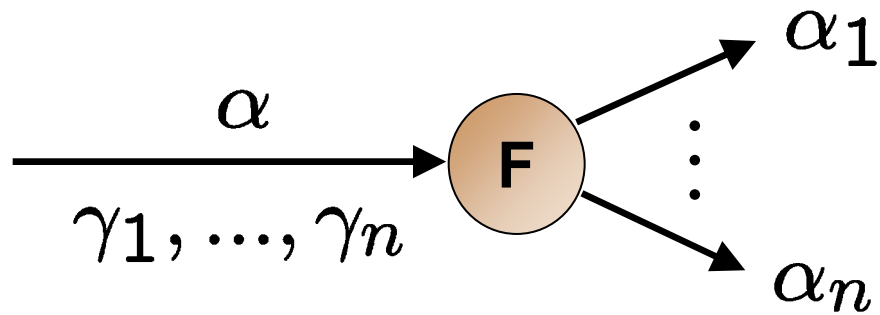
For a fixed number of events in the structured stream the lower (upper) ECC  $\gamma_i^l$  ( $\gamma_i^u$ ) bounds the min (max) number of events of type i.



# Event Count Curves

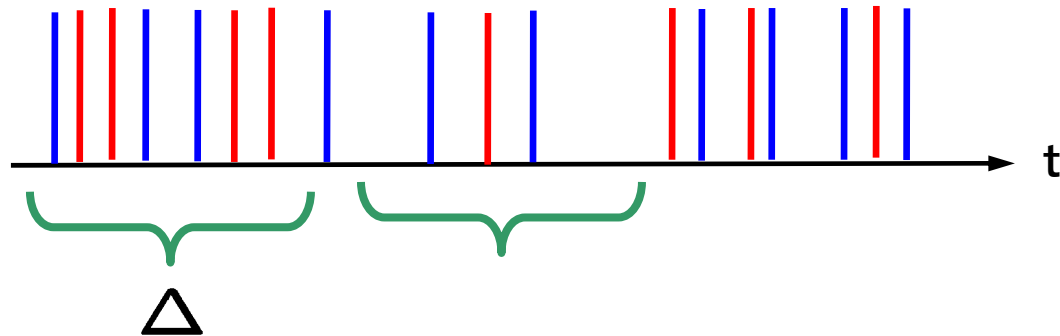


# Fork (Simple Event Streams)



$$\alpha_i^l(\Delta) = \gamma_i^l(\alpha^l(\Delta))$$

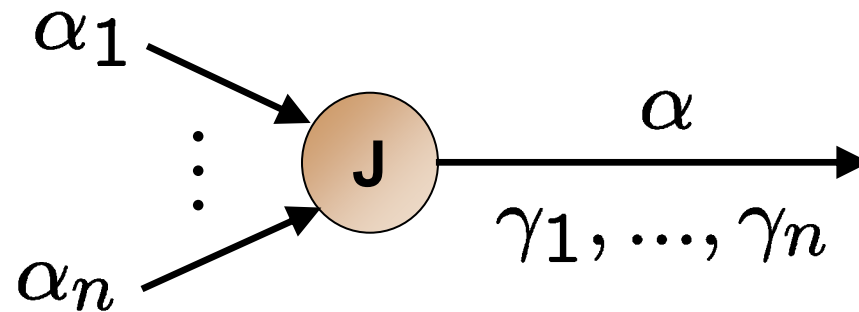
$$\alpha_i^u(\Delta) = \gamma_i^u(\alpha^u(\Delta))$$



$$\gamma_1^l(\alpha^l(\Delta)) = 1$$

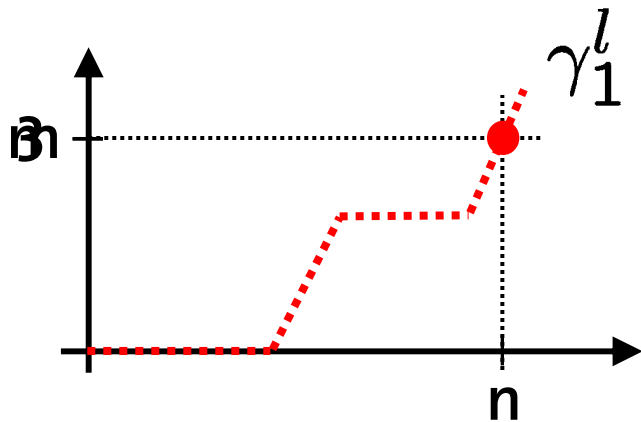
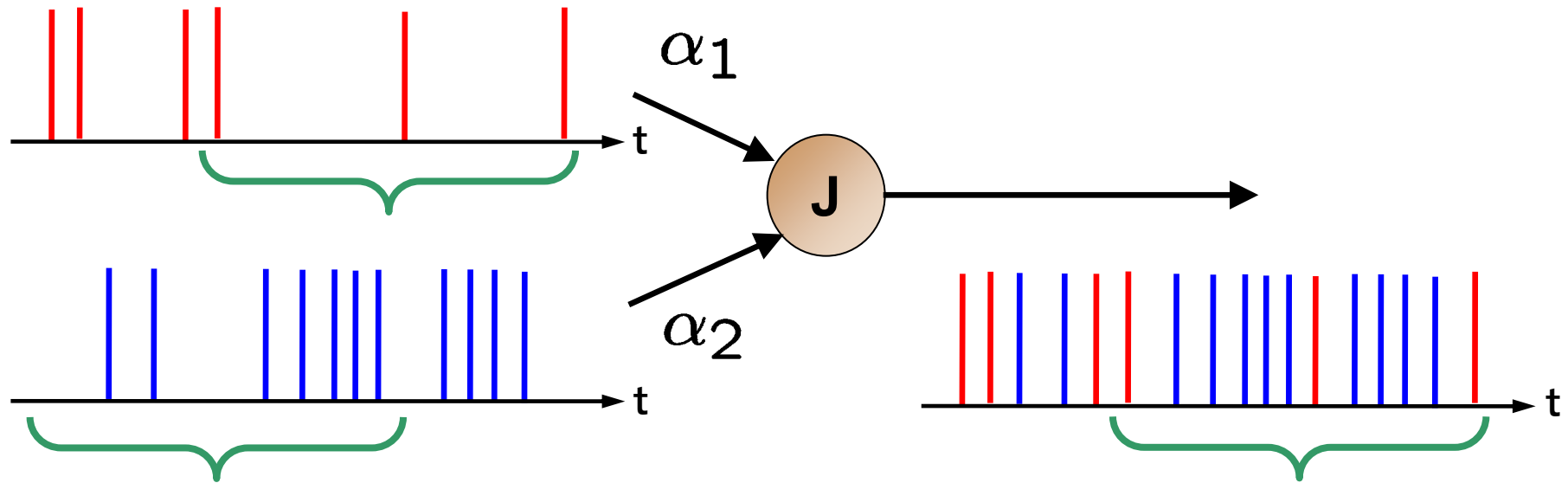
# Join (Simple Event Streams)

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$$\alpha^l(\Delta) = \sum_i \alpha_i^l \quad ; \quad \alpha^u(\Delta) = \sum_i \alpha_i^u$$

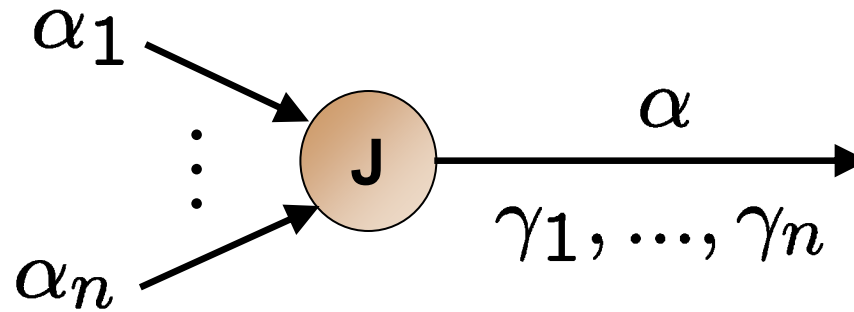
# Join (Simple Event Streams)



$$n = 3 + \alpha_2^u(\alpha_1^{-l}(3)) = 12$$

$$\gamma_1^l(12) = 3$$

# Join (Simple Event Streams)

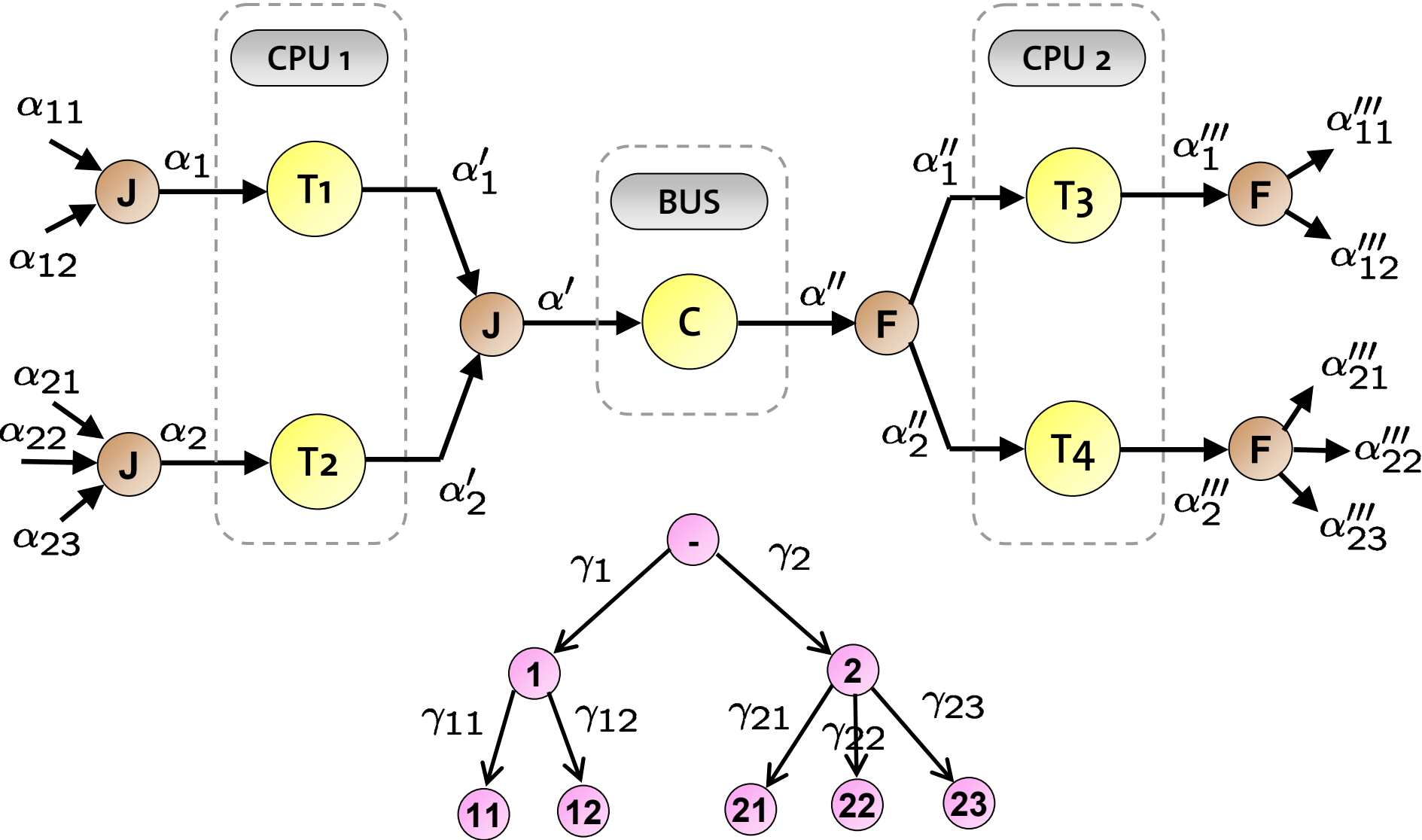


$$\alpha^l(\Delta) = \sum_i \alpha_i^l \quad ; \quad \alpha^u(\Delta) = \sum_i \alpha_i^u$$

$$\begin{aligned} \gamma_i^l(n) &= \epsilon_i^{-u}(n) & \epsilon_i^u(n_i) &= n_i + \sum_{j \neq i} \alpha_j^u(\alpha_i^{-l}(n_i)) \\ \gamma_i^u(n) &= \epsilon_i^{-l}(n) & \epsilon_i^l(n_i) &= n_i + \sum_{j \neq i} \alpha_j^l(\alpha_i^{-u}(n_i)) \end{aligned}$$



# Hierarchical application of ECCs

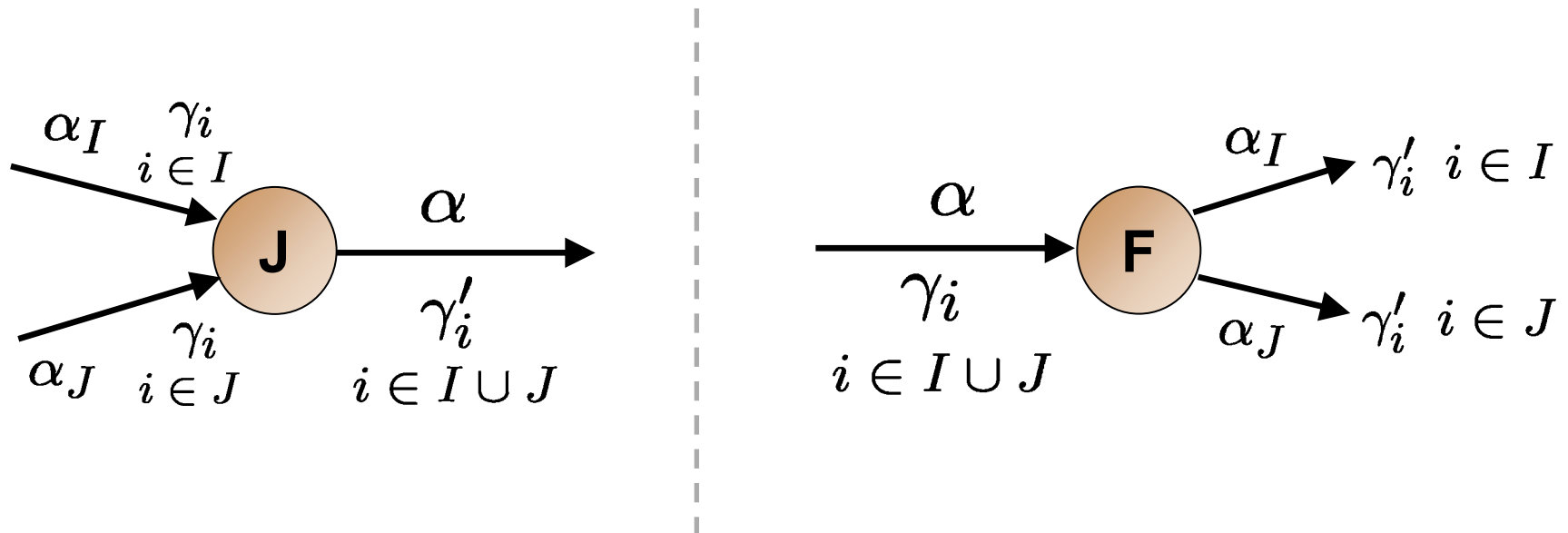


# Arbitrary Join and Fork of Structured Streams

Limitation of hierarchical ECC organization:

Structured streams can be decomposed only in the way they have been composed!

⇒ More general join/fork operators are desirable

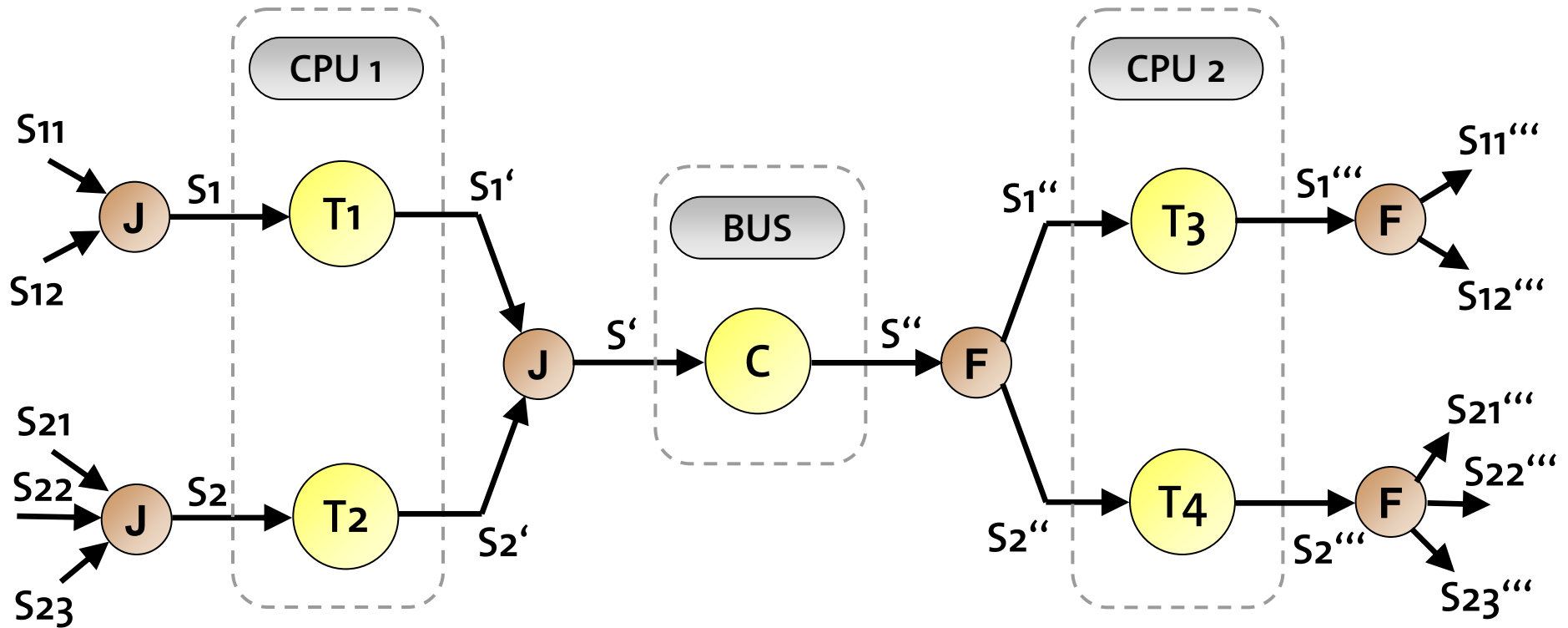


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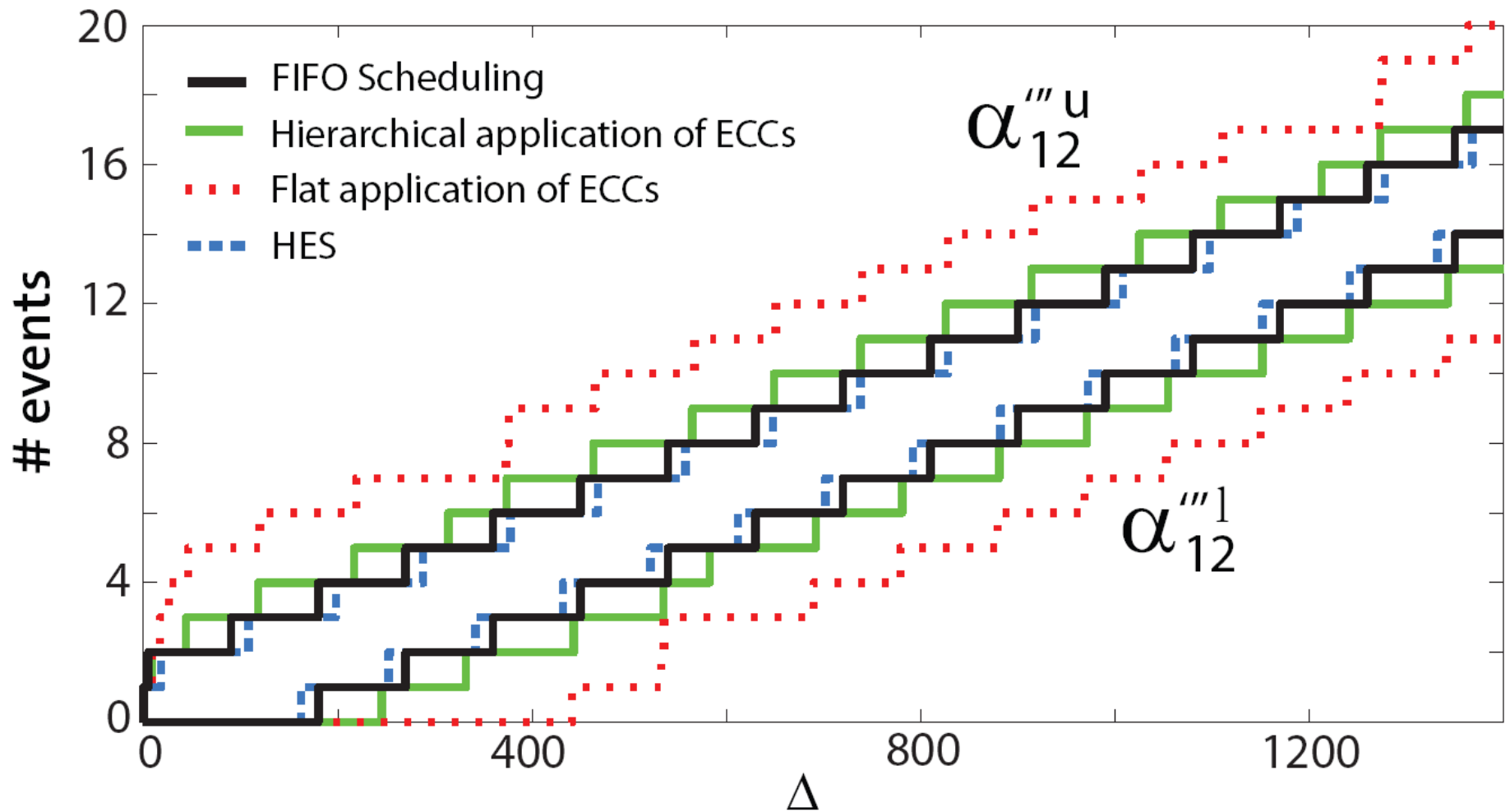
# Example



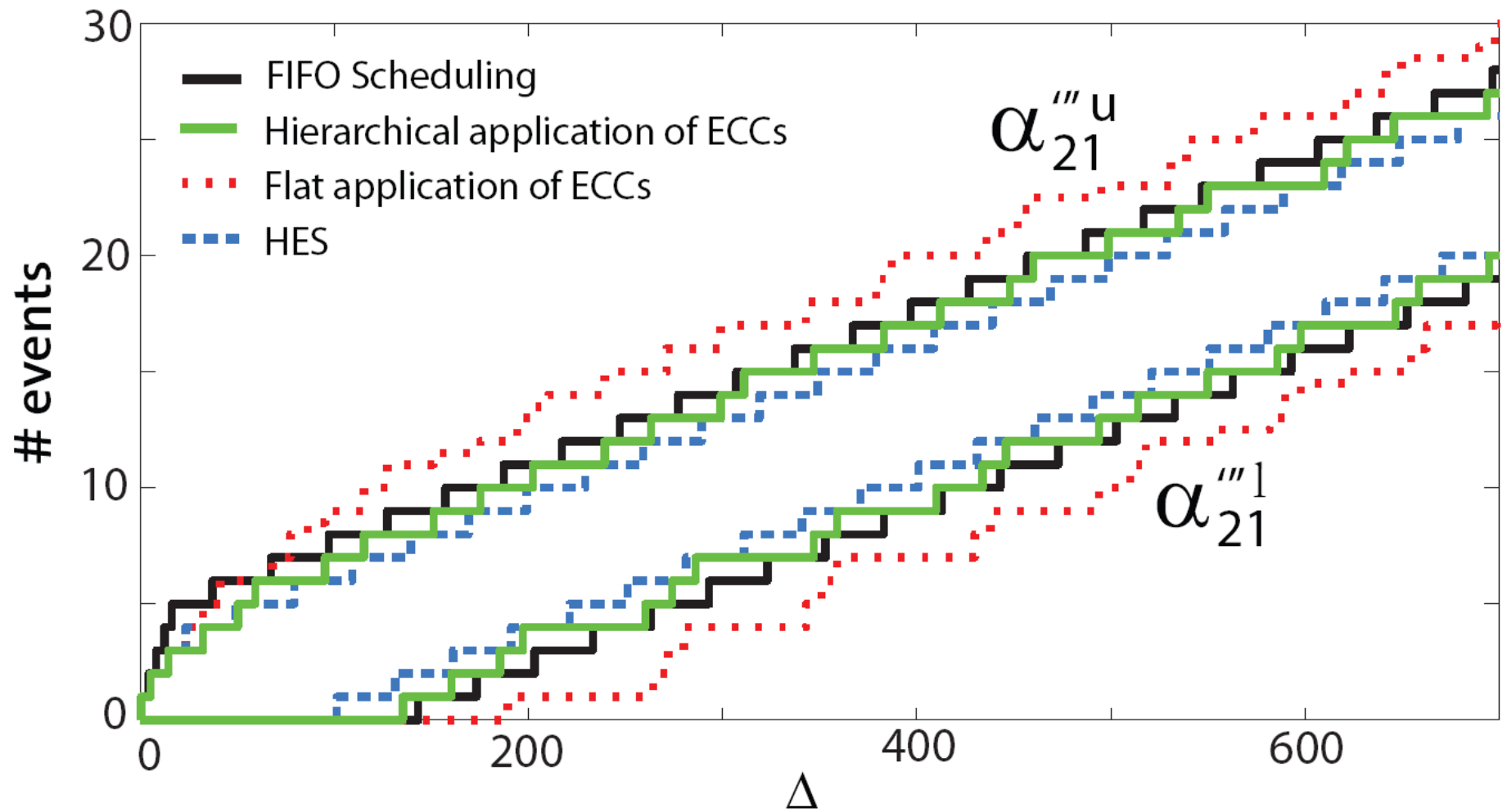
Stream	Period	Jitter
S11	100	30
S12	90	15
S21	30	0
S22	80	20
S23	75	5

Task	BCET	WCET
T1	2	3
T2	3	4
C	9	12
T3	2	3
T4	4	5

# Analysis Results

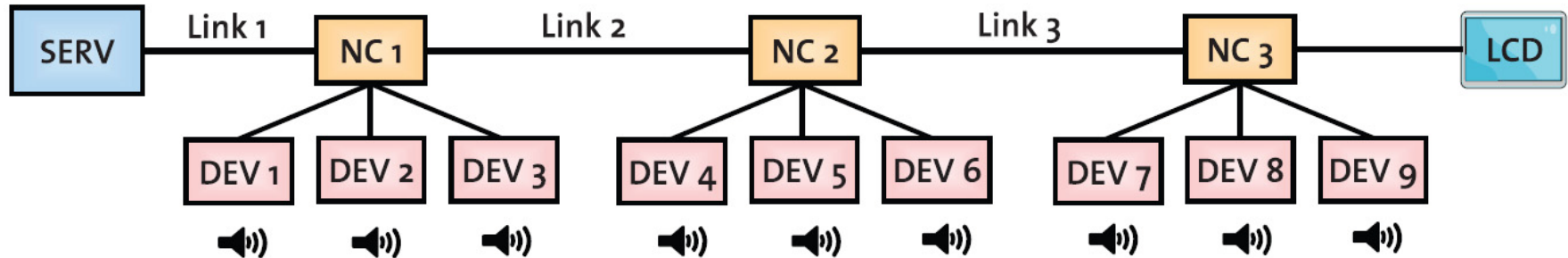


# Analysis Results



# Case Study: Specification

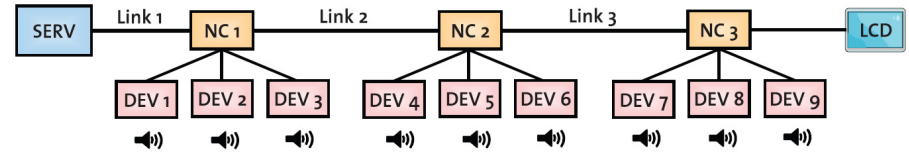
Distributed information/entertainment application



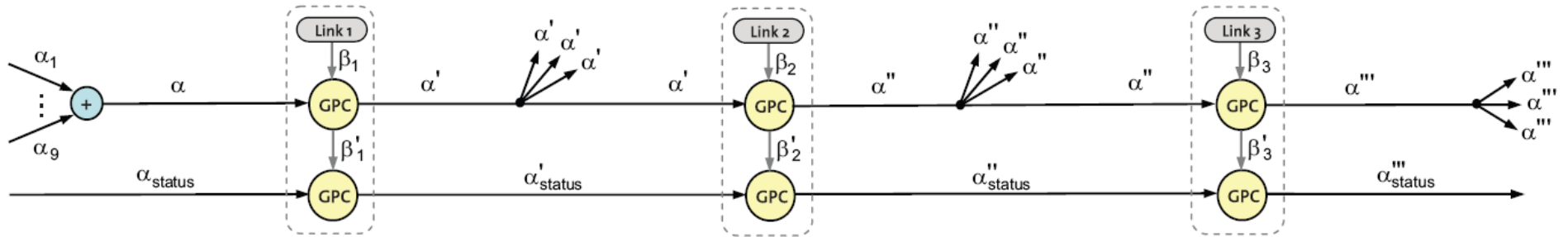
- 2 classes of network traffic:
- On-demand audio streaming (high prior.)
  - Real-time status information (low prior.)

	Size	Period	Jitter	Deadline
<b>Audio Frames</b>	1'518 Bytes	30 ms	5 ms	100 ms
<b>Status Frames</b>	106'500 Bytes	5 s	0 s	1.5 s

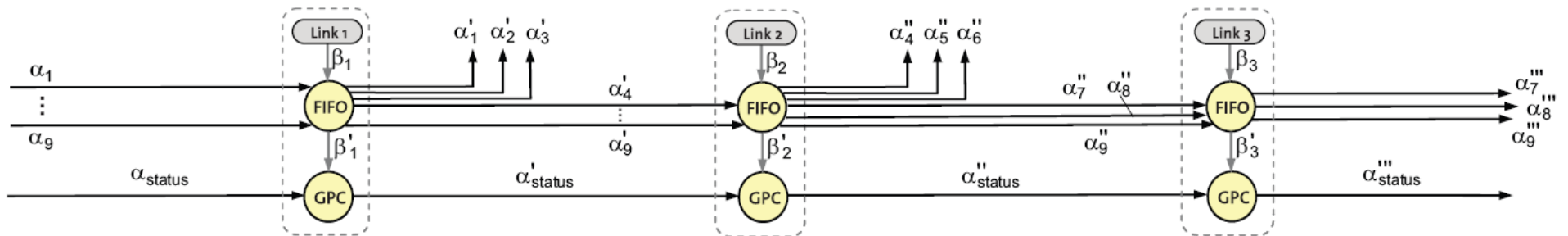
# Case Study: Models (1)



## Classic MPA

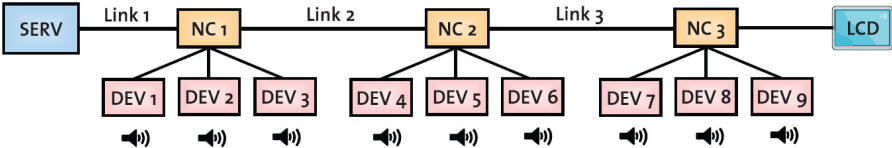


## FIFO components

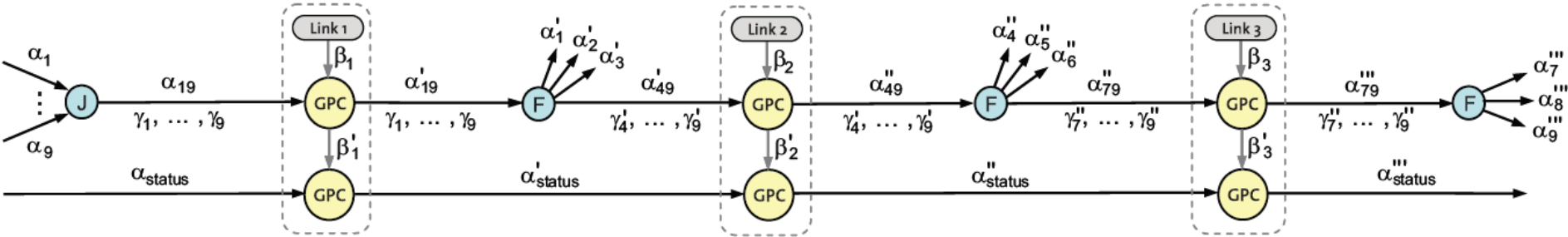




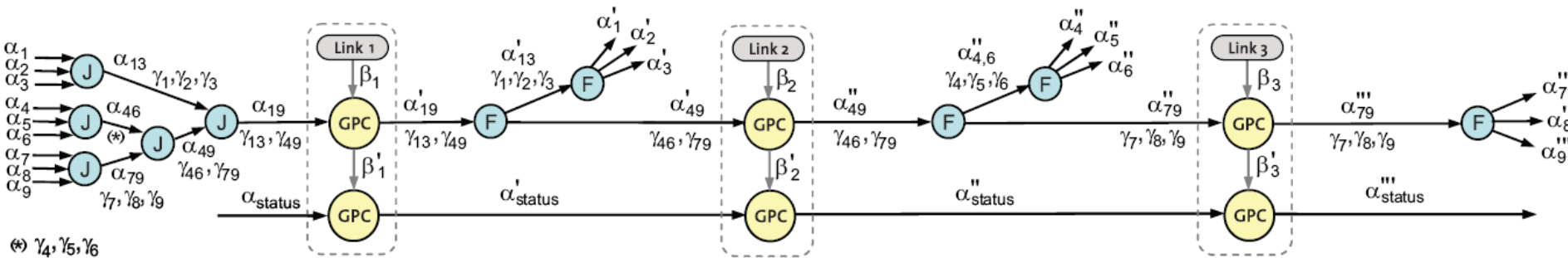
# Case Study: Models (2)



ECC (flat)

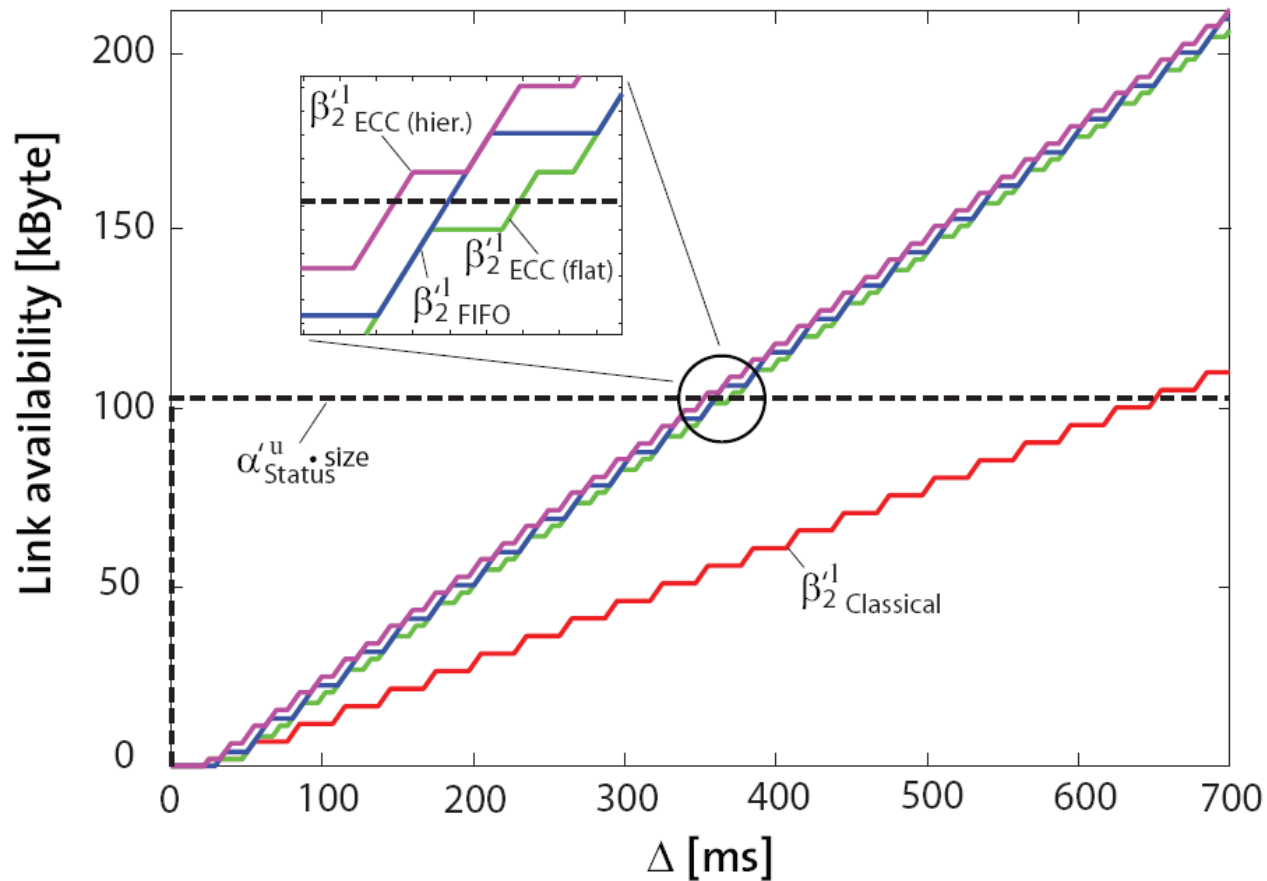


ECC (hierarchic)



# Case Study: Results

	Classic	FIFO	ECC (flat)	ECC (hierar.)
<b>Max. delay</b>	1.954 s	1.255 s	1.316 s	1.248 s



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# Conclusion

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- Two new methods for modeling and analysis of joined event streams in modular performance analysis
- The concept of Event Count Curves is orthogonal to existing event stream models (PJD, arrival curves) and transparent to all analysis components  $\Rightarrow$  Compositionality of methods is not affected
- ECC operators for structured streams allow *arbitrary* decomposition of streams
- Comparisons and Case Study highlight the utility of the proposed methods

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# Thank you!

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